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Third Semester B.E. Degree Examination, Dec.2023/Jan.2024 Engineering Electromagnetics

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. State vector form of Coloumb's law of force between two point charges and indicate the units of the quantities in the equation. (04 Marks)
- b. Let a point charge $Q_1 = 25\text{nC}$ be located at $A(4, -2, 7)$ and charge $Q_2 = 60\text{nC}$ be at $B(-3, 4, -2)$. Find \vec{E} at $C(1, 2, 3)$ and find the direction of \vec{E} . (10 Marks)
- c. Define Electric Field intensity due to number of point charge in a vector form. (02 Marks)

OR

- 2 a. Derive an expression for the electric field intensity due infinite line charge. (06 Marks)
- b. Define electric flux density. Find \vec{D} in Cartesian co-ordinate system at a point $p(6, 8, -10)$ due to a point charge of 40mC at the origin and a uniform line charge of $\rho_L = 40\mu\text{C/m}$ on the z-axis. (10 Marks)

Module-2

- 3 a. State and prove Gauss law and derive first Maxwell's equations from it. (05 Marks)
- b. Given a $60\mu\text{C}$ point charge located at the origin. Find the total electric flux passing through the closed surface defined by $\rho = 26\text{ cm}$ and $z = \pm 26\text{ cm}$. (04 Marks)
- c. State and prove the Divergence theorem. (05 Marks)
- d. Given the electric flux density $D = 0.3r^2\hat{a}_r$, nc/m^2 in free space. Find E at the point $P(r = 2, \theta = 25^\circ, \phi = 90^\circ)$. (02 Marks)

OR

- 4 a. Prove that the work done in moving a charge in the electric field is (06 Marks)

$$W = -Q \int_{\text{initial}}^{\text{final}} E \cdot d\ell.$$
- b. Calculate the work done in moving a 4C charge from $B(1, 0, 0)$ to $A(0, 2, 0)$ along the path $y = 2 - 2x, z = 0$ in the field $E = (5x\hat{a}_x + 5y\hat{a}_y)\text{ V/m}$. (05 Marks)
- c. Show that $\nabla \cdot \mathbf{J} = -\frac{\partial \rho_v}{\partial t}$ with usual notations. (05 Marks)

Module-3

- 5 a. State and explain Biot-Savart's law. (05 Marks)
- b. Two parallel conducting discs are separated by distance 5mm at $z = 0$ and $z = 5\text{mm}$. If $v = 0$ at $z = 0$ and $v = 100\text{v}$ at $z = 5\text{mm}$, find the charge densities on the discs. (05 Marks)
- c. Using Poisson's equation obtain the expression for the junction potential in a p-n junction. (06 Marks)

OR

- 6 a. Derive Laplace and Poisson's equation starting from the Gauss's law and also write Laplace's equation in Cartesian, cylindrical and spherical coordinate system. (08 Marks)
- b. Evaluate both sides of the Stoke's theorem for the field $\vec{H} = 6xy \hat{a}_x - 3y^2 \hat{a}_y$ A/m and the rectangular path around the region $2 \leq x \leq 5$, $-1 \leq y \leq 1$, $z = 0$ let the positive direction of \vec{ds} be \hat{a}_z . (08 Marks)

Module-4

- 7 a. The field $\vec{B} = (-2a_x + 3a_y + 4a_z)$ mT is present in free space. Find the vector force exerted on a straight wire carrying a current of 12A in the a_{AB} direction. Given $A(1, 1, 1)$ and $B(2, 1, 1)$. (04 Marks)
- b. Two differential current elements, $I_1 \Delta L_1 = 3 \times 10^{-6}$ A-m at $P_1(1, 0, 0)$ and $I_2 \Delta L_2 = 3 \times 10^{-6} (-0.5 \hat{a}_x + 0.4 \hat{a}_y + 0.3 \hat{a}_z)$ A-m at $P_2(2, 2, 2)$ are located in free space. Find the vector force exerted on $I_2 \Delta L_2$ by $I_1 \Delta L_1$. (06 Marks)
- c. Find the magnetization in a magnetic material where
- $\mu = 1.8 \times 10^{-5}$ H/m and $H = 120$ A/m.
 - $\mu_r = 22$, there are 8.3×10^{22} atoms/m³ and each atom has a dipole moment of 4.5×10^{-27} A/m².
 - $B = 300 \mu\text{T} \times \chi_m = 15$. (06 Marks)

OR

- 8 a. Derive the Magnetic Boundary Condition? (06 Marks)
- b. Let the permittivity is $5\mu\text{H/m}$ in the region 1 where $x < 0$ and $20 \mu\text{H/m}$ in the region 2 where $x > 0$, and if $\vec{H} = (300a_x - 400a_y + 500a_z)$ A/m and if there is a surface current density $\vec{K} = (150a_y - 200a_z)$ A/m at $x = 0$.
- Find i) $|H_{t_1}|$ ii) $|H_{N_1}|$ iii) $|H_{t_2}|$ iv) $|H_{N_2}|$. (06 Marks)
- c. Derive the expression for the energy density in a magnetic field. (04 Marks)

Module-5

- 9 a. Explain Displacement current density and conduction current density. (04 Marks)
- b. List Maxwell's equations for steady and time varying fields in
- Point form
 - Integral form. (06 Marks)
- c. Do the fields $\vec{E} = E_m \sin x \sin t \hat{a}_y$ and $\vec{H} = \frac{E_m}{\mu_0} \cos x \cos t \hat{a}_z$ satisfy Maxwell's equations? (06 Marks)

OR

- 10 a. What is Forward travelling wave and Backward travelling wave in free space? (02 Marks)
- b. A uniform plane wave in free space is given by $E_s = 200 \angle 30^\circ \cdot e^{-j250z} \hat{a}_x$ V/m.
- Find β , w , f , λ , η , $|\vec{H}|$. (06 Marks)
- c. State and prove Poynting theorem. (08 Marks)
